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1) $\frac{1}{2} \cdot b \cdot h$
 $\frac{1}{2} \cdot 34 \cdot 57.6$
 $= 979.2 \text{ ft}^2$

2) $\frac{.576 \text{ ft}}{.34 \text{ ft}}$ } model slant height
 3) } model base

4) $\frac{1}{2} b h$
 $= \frac{1}{2} \cdot 576 \cdot 34$
 $= .09792 \text{ ft}^2$

5) $\frac{.09792}{979.2}$
 $\frac{1}{10,000} = \left(\frac{1}{100}\right)^2$

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8-6

Changes in Dimensions

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BFE

~~Surface Area Changes:~~

$$S.A. \cdot (\text{scale factor})^2$$

Volume Changes:

$$V \cdot (\text{scale factor})^3$$

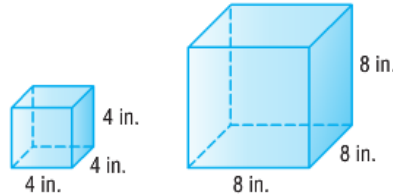
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Surface Area of Similar Solids

If Solid X is similar to Solid Y by a scale factor, then the surface area of X is equal to the surface area of Y times the *square* of the scale factor.

Cubes are **similar solids** because they have the same shape and their corresponding linear measures are proportional.

The cubes at the right are similar. The ratio of their corresponding edge lengths is $\frac{8}{4}$ or 2. The scale factor is 2. How are their surface areas related?



S.A. of Small Cube

$$\text{S.A.} = 6(4 \cdot 4)$$

There are 6 faces.

S.A. of Large Cube

$$\begin{aligned} \text{S.A.} &= 6(2 \cdot 4)(2 \cdot 4) \\ &= 2 \cdot 2(6)(4 \cdot 4) \\ &= 2^2(6)(4 \cdot 4) \end{aligned}$$

To find the surface area of the large cube, multiply the surface area of the small cube by the *square* of the scale factor, 2^2 or 4. This relationship is true for any similar solids.

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- The surface area of a triangular prism is 34 square inches. What is the surface area of a similar prism that is twice as large?
- The world's largest box of raisins has a surface area of 352 square feet. If a similar box is smaller than the largest box by a scale factor of $\frac{1}{48}$, what is its surface area?

$$\begin{aligned} \text{a.) } \text{S.A.} &= 34 \\ &\text{twice as big } (k=2) \end{aligned}$$

$$34 \cdot 2^2 = 136 \text{ in}^2$$

$$\begin{aligned} \text{b.) } \text{SA} &= 352 \\ \text{scale factor} &= \frac{1}{48} \end{aligned}$$

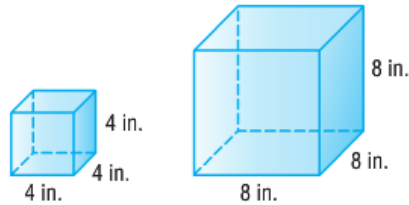
$$\begin{aligned} 352 \cdot \left(\frac{1}{48}\right)^2 &= .15 \text{ ft}^2 \\ &= \frac{11}{72} \text{ ft}^2 \end{aligned}$$

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Volume of Similar Solids

If Solid X is similar to Solid Y by a scale factor, then the volume of X is equal to the volume of Y times the *cube* of the scale factor.

Refer to the cubes below.



Volume of Small Cube

$$V = 4 \cdot 4 \cdot 4$$

Volume of Large Cube

$$\begin{aligned} V &= (2 \cdot 4)(2 \cdot 4)(2 \cdot 4) \\ &= 2 \cdot 2 \cdot 2(4 \cdot 4 \cdot 4) \\ &= 2^3(4 \cdot 4 \cdot 4) \end{aligned}$$

The volumes of similar solids are related by the *cube* of the scale factor.

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- c. A square pyramid has a volume of 512 cubic centimeters. What is the volume of a square pyramid with dimensions one-fourth of the original?
- d. A cylinder has a volume of 432 cubic meters. What is the volume of a cylinder with dimensions one-third of the original?

$$\begin{aligned} \text{c.) } V &= 512 \\ \text{scale} &= \frac{1}{4} \end{aligned}$$

$$512 \cdot \left(\frac{1}{4}\right)^3 = 8 \text{ cm}^3$$

$$\text{d.) } V = 432$$

$$\text{scale} = \frac{1}{3}$$

$$432 \cdot \left(\frac{1}{3}\right)^3 = 16 \text{ m}^3$$

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The surface area of a rectangular prism is 35 square inches. What is the surface area of a similar solid that has been enlarged by a scale factor of 7? (Example 1) _____

$$35 \cdot 7^2$$
$$1715 \text{ in}^2$$

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The volume of a cylinder is about 425 cubic centimeters. What is the volume, to the nearest tenth, of a similar solid that is smaller by a scale factor of $\frac{1}{3}$? (Example 2) _____

$$425 \cdot \left(\frac{1}{3}\right)^3$$
$$\approx 15.7 \text{ cm}^3$$

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A sink with a sliding lid in Josh's art studio measures 16 inches by 15 inches by 6 inches. A second sink used just for paintbrushes has a similar shape and is smaller by a scale factor of $\frac{1}{2}$. Find the volume and surface area of the second sink. (Example 3)

Volume	Surface Area
$V = 16 \cdot 15 \cdot 6$	$2l^2 + Ph$
$= 1440$	$852 \cdot \left(\frac{1}{2}\right)^2$
$1440 \cdot \left(\frac{1}{2}\right)^3 =$	213 in^2
180 in^3	

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O.T.L.

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